

2D finite element program for stress analysis and support design around excavations in soil and rock

# Slope Stability Verification Manual Part II

© 1989 – 2020 Rocscience Inc.

TABLE OF CONTENTS

35 SUBMERGED SLOPE	92
36 SEEPAGE ANALYSIS HOMOGENEOUS SLOPE	94
37 SEEPAGE ANALYSIS OF EARTH EMBANKMENT WITH LAYERED FOUNDATION	98
38 COHESIONLESS EARTH EMBANKMENT WITH SATURATED CLAY FOUNDATION	100
39 EARTH EMBANKMENT WITH INFINITE SLOPE MECHANISM	102
40 SEEPAGE ANALYSIS OF A DAM WITH IMPERMEABLE FOUNDATION	104
41 EARTH EMBANKMENT WITH INFINITE SLOPE MECHANISM	108
42 PLANNED CROSS SECTION OF JAMES DIKE	111
43 EARTH EMBANKMENT WITH INFINITE SLOPE MECHANISM II	113
44 SEEPAGE ANALYSIS FOR AN EARTH EMBANKMENT	116
45 EARTH EMBANKMENT WITH VARYING UNDRAINED SHEAR STRENGTH PROFILE	S 118
46 EARTH EMBANKMENT WITH VARYING UNDRAINED SHEAR STRENGTH PROFILE	S II 121
47 SIMPLE PURELY COHESIVE SLOPE WITH VARYING THICKNESS	126
48 MULTI-TIERED WALL (3 TIERS)	131
49 MULTI-TIERED WALL (EFFECTS OF FILL QUALITY)	134
50 MULTI-TIERED WALL (EFFECTS OF REINFORCEMENT LENGTH)	137
51 MULTI-TIERED WALL (EFFECTS OF REINFORCEMENT TYPE)	140
52 MULTI-TIERED WALL (EFFECTS OF FOUNDATION STRENGTH)	143
53 MULTI-TIERED WALL (EFFECTS OF WATER SEEPAGE)	146
54 MULTI-TIERED WALL (EFFECTS OF SURCHARGE)	149

55 MULTI-TIERED WALL (EFFECTS OF TIER NUMBERS)	152
56 HOMOGENEOUS SLOPE, COMPARISON WITH Z-SOIL, PLAXIS AND GEO FEM	155
57 HOMOGENEOUS SLOPE, COMPARISON WITH Z-SOIL, PLAXIS AND GEO FEM II	166
58 HOMOGENEOUS SLOPE, COMPARISON WITH Z-SOIL, PLAXIS AND GEO FEM III	179
REFERENCES	192

# 35 Submerged slope

#### Introduction

This problem is taken from Figure 6.27 on page 88 of Duncan and Wright (2005).

#### Description

Verification problem #70 for Slide2– a submerged slope with water table at 30 feet above the crest – is shown in Figure 1. The slope is homogeneous with soil properties given in Table 1. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**

# $\begin{array}{c|c} c^{\circ} (psf) & \phi^{\circ} (^{0}) & \gamma (pcf) \\ \hline 100 & 20 & 128 \end{array}$

#### **Table 1 Material Properties**

Figure 1 - Geometry

#### Results

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
OSSR	1.	64
Bishop	1.60	1.56
Spencer	1.60	1.62
GLE	1.60	1.62

Note: Referee Factor of Safety = 1.60 [Duncan and Wright]



Figure 2 – Maximum Shear Strain Plot



Figure 3 – SSR Convergence Graph

#### 36 Seepage analysis homogeneous slope

#### Introduction

This problem is taken from Figure 6.37 on page 100 of Duncan and Wright (2005).

#### Description

Verification problem #71 for Slide2 – a homogeneous slope with water level located at 75 feet at the right end – is shown in Figure 1. The soil properties are given in Table 1. Seepage analysis was carried out using two different methods in this verification problem. The first method was using Finite Element seepage analysis and the second method was using piezometric line approximation. The location of the approximated piezometric line is shown in Figure 2. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**

#### Table 1 Material Properties

c (psf)	φ ( <sup>0</sup> )	γ (pcf)
200	20	125



#### **Figure 1 - Geometry**



Figure 2 – Approximated Piezometric Line Location

#### Results

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	1.	12
Bishop	1.139	1.046
Spencer	1.138	1.128
GLE	1.140	1.109

**Case 1: Finite Element Seepage Analysis** 

Note: Referee Factor of Safety = 1.138 [Duncan and Wright]



**Figure 3 – Pore Water Pressure Plot** 



Figure 4 – Maximum Shear Strain Plot

Shear Strength Reduction Critical SRF: 1.12 at Displacement: 0.175 ft



Figure 5 – SSR Convergence Graph

Case 2.	Piezometric	Line A	nnr	ovimation	Seenage	Analysis
Case 2.	I lezometi ic	LINC P	zhhr	oximation	Seepage	Analysis

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	1.	12
Bishop	1.142	1.081
Spencer	1.140	1.147
GLE	1.141	1.154

Note: Referee Factor of Safety = 1.141 [Duncan and Wright]



**Figure 6 – Pore Water Pressure Plot** 



Figure 7 – Maximum Shear Strain Plot



Figure 8 – SSR Convergence Graph

This problem is taken from Figure 6.39 on page 101 of Duncan and Wright (2005).

#### Description

Verification problem #72 – a symmetric earth embankment dam resting on a layered soil foundation with ponded water of elevation 302 feet on the left side – is shown in Figure 1. Both left face and right face are constructed using shell material. Seepage analysis was performed in this verification problem. The material strength properties and permeability values are given in Table 1. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**

Material	k (ft/s)	c' (psf)	φ' ( <sup>0</sup> )	γ (pcf)
Outer Shell	1.67 x 10 <sup>-4</sup>	0	34	125
Clay Core	1.67 x 10 <sup>-8</sup>	100	26	122
Foundation Clay	1.67 x 10 <sup>-7</sup>	0	24	123
Foundation Sand	1.67 x 10 <sup>-5</sup>	0	32	127

#### **Table 1 Material Properties**



**Figure 1 - Geometry** 

#### Results

Method	Factor of Safety (circular)	Factor of Safety (non-circular)	
SSR	0.95		
Bishop	1.15	1.05	
Spencer	1.16	1.20	
GLE	1.16	1.21	

Note: Referee Factor of Safety = 1.11 [Duncan and Wright]



**Figure 2 – Pore Water Pressure Plot** 



Figure 3 – Maximum Shear Strain Plot

Shear Strength Reduction - Critical SRF: 1.1 at Displacement: 0.776 ft



**Figure 4 – SSR Convergence Graph** 

# 38 Cohesionless Earth Embankment with Saturated Clay Foundation

#### Introduction

This problem is taken from Figure 7.12 on page 120 of Duncan and Wright (2005).

#### Description

Verification problem #74 for Slide2 – an embankment of cohesionless material resting on saturated clay foundation – is shown in Figure 1. The material properties are given in Table 1. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**

Material	c (psf)	φ ( <sup>0</sup> )	γ (pcf)
Embankment (Sand)	0	40	140
Foundation (Saturated Clay)	2500	0	140







#### Results

Method	Factor of Safety (circular)	Factor of Safety (non-circular)	Referee Factor of Safety [Duncan and Wright]
SSR	1.21		
Bishop	1.23	1.09	1.22
Janbu Simplified	1.08	1.04	1.07
Janbu Corrected	1.18	1.13	1.16
Spencer	1.20	1.18	1.19



Figure 2 – Maximum Shear Strain Plot

Shear Strength Reduction Critical SRF: 1.21 at Displacement: 0.910 ft

1.5 1.4 Strength Reduction Factor 1.3 **¢** Converged Failed to Converge 1.1 1.0 12 16 0 1 11 13 14 15 2 3 6 7 8 9 10 Maximum Total Displacement [ft] 4 5

Figure 3 – SSR Convergence Graph

# 39 Earth Embankment with Infinite Slope Mechanism

#### Introduction

This problem is taken from Figure 7.19 on page 128 of Duncan and Wright (2005).

#### Description

Verification problem #76 for Slide2 – a symmetric homogeneous earth embankment resting on an impermeable foundation with a ponded water of elevation 40 feet on its left side – is shown in Figure 1. The material properties and permeability values are given in Table 1. Seepage analysis was conducted in this verification problem. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**



#### **Table 1 Material Properties**





#### Results

Method	Factor of Safety (circular)
SSR	0.97
Bishop	1.07
Spencer	1.08
GLE	1.08

Note: Referee Factor of Safety = 1.08 - 1.19 [Duncan and Wright]







Figure 3 – Maximum Shear Strain Plot



Figure 4 – SSR Convergence Graph

This problem is taken from Figure 7.24 on page 131 of Duncan and Wright (2005).

#### Description

Verification problem #77 for Slide2 – a symmetric earth dam with thick core and with ponded water of elevation 315 on its left side resting on an impervious foundation – is shown in Figure 1. The material properties are given in Table 1. Seepage analysis was performed using two different techniques in this verification problem. The first technique was using Finite Element seepage analysis and the second technique was using piezometric line approximation. The location of the approximated piezometric line is shown in Figure 2. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**

Zone	c' (psf)	φ' ( <sup>0</sup> )	γ (pcf)	k (ft/s)
Core	0	20	120	1.67x 10 <sup>-7</sup>
Shell	0	38	140	1.67x 10 <sup>-5</sup>

**Table 1 Material Properties** 



Figure 1 - Geometry



**Figure 2 – Approximated Piezometric Line Location** 

### Results

Method	Factor of Safety (circular)	Factor of Safety (non-circular)	Referee Factor of Safety [Duncan and Wright]
SSR	1.52		
Bishop	1.58	1.49	1.62
Spencer	1.64	1.57	1.69





**Figure 3 – Pore Water Pressure Plot** 



Figure 4 – Maximum Shear Strain Plot



**Figure 5 – SSR Convergence Graph** 

#### Case 2: Piezometric Line Approximation Seepage Analysis

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	1.53	
Bishop	1.58	1.48
Spencer	1.65	1.57
GLE	1.66	1.57

Note: Referee Factor of Safety = 1.67 [Duncan and Wright]



**Figure 6 – Pore Water Pressure Plot** 



Figure 7 – Maximum Shear Strain Plot



Figure 8 – SSR Convergence Graph

This problem is taken from Figure 14.4 on page 217 of Duncan and Wright (2005).

#### Description

Verification problem #79 for Slide2 – a cohesionless earth embankment – is shown in Figure 1. Two slip surfaces are of interest in this verification problem. The first is slip surface that is very shallow (infinite slope mechanism) and the second is deep slip surface. In order to get the first slip surface, it was assumed that the slip surface would not go through the boundary between the embankment and its foundation. To prevent the slip surface from crossing that boundary, the foundation was considered as elastic material in the analysis. The material properties are given in Table 1. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**

Zone	c' (psf)	φ' ( <sup>0</sup> )	γ (pcf)
Embankment	0	30	120
Foundation	450	0	120

#### Table 1 Material Properties



#### **Figure 1 - Geometry**

#### **Results – Very Shallow Slip Surface (Infinite Slope Mechanism)**

Method	Factor of SafetyFactor of Safety(circular)(non-circular)	
SSR	1.47	
Bishop	1.44	1.44
Spencer	1.44	1.44
GLE	1.44	1.44

Note: Referee Factor of Safety = 1.44 [Duncan and Wright]



Figure 2 – Maximum Shear Strain Plot (Very Shallow Slip Surface)



Figure 3 – SSR Convergence Graph (Very Shallow Slip Surface)

# **Results – Deep Slip Surface**

Method	Factor of SafetyFactor of Safety(circular)(non-circular)	
SSR	1.43	
Bishop	1.41	1.23
Spencer	1.40	1.36
GLE	1.40	1.38

Note: Referee Factor of Safety = 1.40 [Duncan and Wright]



Figure 4 – Maximum Shear Strain Plot (Deep Slip Surface)



Figure 5 – SSR Convergence Graph (Deep Slip Surface)

This problem is taken from Figure 7.16 on page 124 of Duncan and Wright (2005).

#### Description

Verification problem #75 for Slide2 – the planned cross section of James Dike – is shown in Figure 1. The material properties are given in Table 1. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**

Material	c (kN/m <sup>2</sup> )	φ ( <sup>0</sup> )	$\gamma$ (kN/m <sup>3</sup> )
Fill	0	30	20
Clay "crust"	41	0	20
Marine Clay	34.5	0	18.8
Lacustrine Clay	31.2	0	20.3

#### Table 1 Material Properties





#### Results

Method	Factor of Safety (non-circular)
SSR	1.26
Bishop	1.11
Spencer	1.16
GLE	1.15

Note: Referee Factor of Safety = 1.17 [Duncan and Wright]



Figure 2 – Maximum Shear Strain Plot



Figure 3 – SSR Convergence Graph

This problem is taken from Figure 14.7 on page 220 of Duncan and Wright (2005).

#### Description

Verification problem #81 for Slide2 – an earth embankment – is shown in Figure 1. Two slip surfaces are of interest in this verification problem. The first is slip surface that is very shallow (infinite slope mechanism) and the second is deep slip surface. In order to get the first slip surface, it was assumed that the slip surface would not go through the boundary between the embankment and its foundation. To prevent the slip surface from crossing that boundary, the foundation was considered as elastic material in the analysis. The material properties are given in Table 1. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**

Zone	c' (psf)	φ' ( <sup>0</sup> )	γ (pcf)
Embankment	0	30	124
Foundation	500	0	98



#### Figure 1 - Geometry

#### Results - Very Shallow Slip Surface (Infinite Slope Mechanism)

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	1.19	
Bishop	1.15	1.15
Spencer	1.15	1.15
GLE	1.15	1.15

Note: Referee Factor of Safety = 1.15 [Duncan and Wright]

#### **Table 1 Material Properties**



Figure 2 – Maximum Shear Strain Plot (Very Shallow Slip Surface)



Figure 3 – SSR Convergence Graph (Very Shallow Slip Surface)

# **Results – Deep Slip Surface**

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	1.23	
Bishop	1.23	1.08
Spencer	1.21	1.19
GLE	1.22	1.20

Note: Referee Factor of Safety = 1.21 [Duncan and Wright]







Figure 5 – SSR Convergence Graph (Deep Slip Surface)

This problem is taken from Figure 14.20-a on page 230 of Duncan and Wright (2005).

# Description

Verification problem #82 for Slide2 – an earth embankment – is shown in Figure 1. The seepage analysis was carried out using piezometric line approximation technique. The material properties are given in Table 1. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**

#### **Table 1 Material Properties**

Zone	c' (psf)	φ' ( <sup>0</sup> )	γ (pcf)
Embankment	600	25	125
Foundation	0	30	132





#### Results

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	1.	51
Bishop	1.532	1.444
Spencer	1.541	1.535
GLE	1.539	1.526

Note: Referee Factor of Safety = 1.528 – 1.542 [Duncan and Wright]



Figure 2 – Maximum Shear Strain Plot



Figure 3 – SSR Convergence Graph

This problem is taken from Figure 14.20-b on page 230 of Duncan and Wright (2005).

#### Description

Verification problem #83 for Slide2 – an earth embankment – is shown in Figure 2. Two undrained shear strength profiles for its foundation are tested. The material properties are given in Table 1 and the foundation's undrained shear strength profiles are presented in Figure 1. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**

Zone	c' (psf)	<b>φ</b> ' ( <sup>0</sup> )	γ (pcf)
Embankment	0	36	123
Foundation	see Fig. 1	0	97



#### **Figure 1 – Undrained Shear Strength Profiles**



**Figure 2 - Geometry** 

# **Table 1 Material Properties**

Kesuits – Unuraineu Shear Strength Frome.	Results -	- Undrained	Shear	Strength	<b>Profile</b>
---	-----------	-------------	-------	----------	----------------

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	1.	32
Bishop	1.312	1.157
Spencer	1.285	1.263
GLE	1.293	1.269

Note: Referee Factor of Safety = 1.276 – 1.323 [Duncan and Wright]



Critical SRF: 1.32

Figure 3 – Maximum Shear Strain Plot (Undrained Shear Strength Profile I)





**Results – Undrained Shear Strength Profile II** 

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	1.	32
Bishop	1.335	1.068
Spencer	1.329	1.175
GLE	1.331	1.204

Note: Referee Factor of Safety = 1.295 – 1.328 [Duncan and Wright]



Figure 5 – Maximum Shear Strain Plot (Undrained Shear Strength Profile II)



Figure 6 – SSR Convergence Graph (Undrained Shear Strength Profile II)

This problem is taken from Figure 15.9 on page 244 of Duncan and Wright (2005).

#### Description

Verification problem #84 for Slide2 – an earth embankment – is shown in Figure 1. Four undrained shear strength profiles for its foundation are investigated. The undrained shear strength profiles can be generalized as:

$$c_{\mu} = 300 + c_{z} z$$

where z is depth (in feet) and  $c_z$  is the rate of increase in undrained shear strength.  $c_z$  value varies among profiles. The material properties are given in Table 1 and the  $c_z$  values are presented in Table 2. The factor of safety and its corresponding slip surface are required.

#### **Geometry and Properties**

#### **Table 1 Material Properties**

Zone	c' (psf)	φ' ( <sup>0</sup> )	γ (pcf)
Embankment	0	35	125
Foundation	$c_u = 300 + c_z z$	0	100

Table 2 - c<sub>z</sub> Values

Profile	c <sub>z</sub> (psf/ft)
Ι	0
II	5
III	10
IV	15



**Figure 1 - Geometry** 

**Results – Undrained Shear Strength Profile I** 

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	0.	78
Bishop	0.76	0.68
Spencer	0.76	0.74
GLE	0.76	0.75

Note: Referee Factor of Safety = 0.75 [Duncan and Wright]



Figure 2 – Maximum Shear Strain Plot (Undrained Shear Strength Profile I)



Figure 3 – SSR Convergence Graph (Undrained Shear Strength Profile I)

Results -	Undraine	ed Shear	Strength	Profile	II
	· · · · · · · · · · · · · · · · · · ·		~~		

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	0.9	93
Bishop	0.91	0.81
Spencer	0.90	0.91
GLE	0.91	0.92

Note: Referee Factor of Safety = 0.90 [Duncan and Wright]



Figure 4 – Maximum Shear Strain Plot (Undrained Shear Strength Profile II)



Figure 5 – SSR Convergence Graph (Undrained Shear Strength Profile II)

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	1.	05
Bishop	1.04	0.93
Spencer	1.03	1.02
GLE	1.03	1.02

Note: Referee Factor of Safety = 1.03 [Duncan and Wright]



Figure 6 – Maximum Shear Strain Plot (Undrained Shear Strength Profile III)



Figure 7 – SSR Convergence Graph (Undrained Shear Strength Profile III)
Results -	Undrained	l Shear	Strength	<b>Profile IV</b>
-----------	-----------	---------	----------	-------------------

Method	Factor of Safety (circular)	Factor of Safety (non-circular)
SSR	1.	15
Bishop	1.15	1.04
Spencer	1.13	1.12
GLE	1.14	1.12

Note: Referee Factor of Safety = 1.13 [Duncan and Wright]



Figure 8 – Maximum Shear Strain Plot (Undrained Shear Strength Profile IV)



Figure 9 – SSR Convergence Graph (Undrained Shear Strength Profile IV)

This problem is taken from Figure 14.3 on page 216 of Duncan and Wright (2005).

#### Description

Verification problem #78 for Slide2 – a simple, pure cohesive slope – is shown in Figure 1. Three different foundation thicknesses (30 feet-thick, 46.5 feet-thick and 60 feet-thick) are tested. The material properties are given in Table 1. The factor of safety and its corresponding slip surface are required.

# **Geometry and Properties**



#### **Table 1 Material Properties**

**Figure 1 - Geometry** 

#### **Results – 30 feet-thick Foundation**

	Factor of Saf	Easter of Safaty	
Method	Passes Trough the Toe	Touches the Bottom of the Foundation	(non-circular)
SSR	1.03		
Bishop	1.126	1.141	0.904
Spencer	1.200	1.139	1.037
GLE	1.185	1.137	1.082

Note: Referee Factor of Safety = 1.124 (passes through the toe) & 1.135 (touches the bottom of the foundation) [Duncan and Wright]



Figure 2 – Maximum Shear Strain Plot (30 feet-thick Foundation)



Figure 3 – SSR Convergence Graph (30 feet-thick Foundation)

# **Results – 46.5 feet-thick Foundation**

	Factor of Safety (circular)		Eastor of Safaty
Method	Passes Trough the Toe	Touches the Bottom of the Foundation	(non-circular)
SSR		1.02	
Bishop	1.126	1.130	0.882
Spencer	1.201	1.128	1.037
GLE	1.186	1.127	1.082

Note: Referee Factor of Safety = 1.124 (passes through the toe & touches the bottom of the foundation) [Duncan and Wright]



Figure 4 – Maximum Shear Strain Plot (46.5 feet-thick Foundation)





Figure 5 – SSR Convergence Graph (46.5 feet-thick Foundation)

# **Results – 60 feet-thick Foundation**

	Factor of Saf	Eastor of Safaty	
Method	Passes Trough the Toe	Touches the Bottom of the Foundation	(non-circular)
SSR	1.02		
Bishop	1.125	1.125	0.873
Spencer	1.201	1.124	1.062
GLE	1.185	1.122	1.062

Note: Referee Factor of Safety = 1.124 (passes through the toe) & 1.119 (touches the bottom of the foundation) [Duncan and Wright]



Figure 6 – Maximum Shear Strain Plot (60 feet-thick Foundation)



Figure 7 – SSR Convergence Graph (60 feet-thick Foundation)

This problem is taken from the Baseline case studied in the "Geosynthetic Reinforced Multitiered Walls", a paper by Leshchinsky, D. and Han, J. (2004).

# Description

Verification problem #87 for Slide2 – A three-tiered wall – is shown in Figure 1. The material properties are presented in Table 1 and the support properties are shown in Table 2. The shear strength of the support is assumed to equal to 80% of the fill strength.

# **Geometry and Properties**

Fable 1	Material	Properties
---------	----------	------------

Zone	c (kPa)	$\phi$ ( <sup>0</sup> )	$\gamma$ (kN/m <sup>3</sup> )
Reinforced and retained fill	0	34	18
Foundation soil	10	34	18
Blocks	2.5	34	18

Length (m)	Tensile Strength (kN/m)
6.3	10.0



**Figure 1 - Geometry** 

Method	Factor of Safety
SSR	1.05
Bishop	1.02
Spencer	1.03
GLE	1.03

Note: Referee Factor of Safety = 0.99 [Leshchinsky and Han]



Figure 2 – Maximum Shear Strain Plot

#### Shear Strength Reduction Critical SRF: 1.05 at Displacement: 0.118 m



Figure 3 – SSR Convergence Graph

This problem is taken from the Fill Quality case studied in the "Geosynthetic Reinforced Multitiered Walls", a paper by Leshchinsky, D. and Han, J. (2004).

#### Description

Verification problem #88 for Slide2 – A three-tiered wall – is shown in Figure 1. The material properties are presented in Table 1 and the support properties are shown in Table 2. The shear strength of the support is assumed to equal to 80% of the fill strength. The purpose of this verification model is to quantify the effect of fill quality on the stability characteristic of a multi-tiered wall.

# **Geometry and Properties**

Zone	c (kPa)	φ ( <sup>0</sup> )	$\gamma$ (kN/m <sup>3</sup> )
Reinforced and retained fill	0	25	18
Foundation soil	10	34	18
Blocks	2.5	34	18

# **Table 1 Material Properties**

Length (m)	Tensile Strength (kN/m)
6.3	22.0



**Figure 1 - Geometry** 

Method	Factor of Safety
SSR	1.08
Bishop	0.98
Spencer	0.97
GLE	0.97

Note: Referee Factor of Safety = 0.99 [Leshchinsky and Han]



Figure 2 – Maximum Shear Strain Plot

Shear Strength Reduction Critical SRF: 1.08 at Displacement: 0.163 m



Figure 3 – SSR Convergence Graph

This problem is taken from the Reinforcement Length case studied in the "Geosynthetic Reinforced Multitiered Walls", a paper by Leshchinsky, D. and Han, J. (2004).

#### Description

Verification problem #89 for Slide2 – A three-tiered wall – is shown in Figure 1. The material properties are presented in Table 1 and the support properties are shown in Table 2. The shear strength of the support is assumed to equal to 80% of the fill strength. The purpose of this verification model is to quantify the effect of reinforcement length on the stability characteristic of a multi-tiered wall.

# **Geometry and Properties**

Zone	c (kPa)	$\phi$ ( <sup>0</sup> )	$\gamma$ (kN/m <sup>3</sup> )
Reinforced and retained fill	0	34	18
Foundation soil	10	34	18
Blocks	2.5	34	18

# **Table 1 Material Properties**



Figure 1 - Geometry

Method	Factor of Safety
SSR	0.93
Bishop	0.93
Spencer	0.92
GLE	0.91

Note: Referee Factor of Safety = 0.98 [Leshchinsky and Han]



Figure 2 – Maximum Shear Strain Plot

Shear Strength Reduction Critical SRF: 0.93 at Displacement: 0.079 m



Figure 3 – SSR Convergence Graph

This problem is taken from the Reinforcement Type case studied in the "Geosynthetic Reinforced Multitiered Walls", a paper by Leshchinsky, D. and Han, J. (2004).

#### Description

Verification problem #90 for Slide2 – A three-tiered wall – is shown in Figure 1. The material properties are presented in Table 1 and the support properties are shown in Table 2. The shear strength of the supports is assumed to equal to 80% of the fill strength. The purpose of this verification model is to quantify the effect of reinforcement type on the stability characteristic of a multi-tiered wall.

# **Geometry and Properties**

Zone	c (kPa)	$\phi$ ( <sup>0</sup> )	$\gamma$ (kN/m <sup>3</sup> )
Reinforced and retained fill	0	34	18
Foundation soil	10	34	18
Blocks	2.5	34	18

# **Table 1 Material Properties**

Туре	Length (m)	Tensile Strength (kN/m)
#1 (upper 8 layers)	6.3	7.5
#2 (lower 7 layers)	6.3	11.0



Figure 1 - Geometry

Method	Factor of Safety
SSR	1
Bishop	0.92
Spencer	0.91
GLE	0.91

Note: Referee Factor of Safety = 1.01 [Leshchinsky and Han]



Figure 2 – Maximum Shear Strain Plot

Shear Strength Reduction Critical SRF: 1 at Displacement: 0.124 m



Figure 3 – SSR Convergence Graph

This problem is taken from the Foundation Soil case studied in the "Geosynthetic Reinforced Multitiered Walls", a paper by Leshchinsky, D. and Han, J. (2004).

# Description

Verification problem #91 for Slide2– A three-tiered wall – is shown in Figure 1. The material properties are presented in Table 1 and the support properties are shown in Table 2. The shear strength of the support is assumed to equal to 80% of the fill strength. The purpose of this verification model is to quantify the effect of foundation soil strength on the stability characteristic of a multi-tiered wall.

# **Geometry and Properties**

Zone	c (kPa)	$\phi$ ( <sup>0</sup> )	$\gamma$ (kN/m <sup>3</sup> )
Reinforced and retained fill	0	34	18
Foundation soil	0	18	18
Blocks	2.5	34	18

# **Table 1 Material Properties**

Length (m)	Tensile Strength (kN/m)
6.3	10.0



**Figure 1 - Geometry** 

Method	Factor of Safety
SSR	0.84
Spencer	0.96
GLE	0.98

Note: Referee Factor of Safety = 0.86 [Leshchinsky and Han]



Figure 2 – Maximum Shear Strain Plot





Figure 3 – SSR Convergence Graph

This problem is taken from the Water case studied in the "Geosynthetic Reinforced Multitiered Walls", a paper by Leshchinsky, D. and Han, J. (2004).

#### Description

Verification problem #92 for Slide2 – A three-tiered wall – is shown in Figure 1. The material properties are presented in Table 1 and the support properties are shown in Table 2. The shear strength of the support is assumed to equal to 80% of the fill strength. The purpose of this verification model is to quantify the effect of water seepage on the stability characteristic of a multi-tiered wall.

# **Geometry and Properties**

Zone	c (kPa)	$\phi$ ( <sup>0</sup> )	$\gamma$ (kN/m <sup>3</sup> )
Reinforced and retained fill	0	34	18
Foundation soil	10	34	18
Blocks	2.5	34	18

# **Table 1 Material Properties**

# **Table 2 Support Properties**



Figure 1 - Geometry

24 m

Method	Factor of Safety
SSR	1.03
Bishop	0.92
Spencer	1.00
GLE	1.13

Note: Referee Factor of Safety = 1.01 [Leshchinsky and Han]



Figure 2 – Maximum Shear Strain Plot

Shear Strength Reduction Critical SRF: 1.03 at Displacement: 0.123 m



Figure 3 – SSR Convergence Graph

This problem is taken from the Surcharge case studied in the "Geosynthetic Reinforced Multitiered Walls", a paper by Leshchinsky, D. and Han, J. (2004).

#### Description

Verification problem #93 for Slide2 – A three-tiered wall – is shown in Figure 1. The material properties are presented in Table 1 and the support properties are shown in Table 2. The shear strength of the support is assumed to equal to 80% of the fill strength. The purpose of this verification model is to quantify the effect of surcharge on the stability characteristic of a multi-tiered wall.

#### **Geometry and Properties**

Zone	c (kPa)	$\phi$ ( <sup>0</sup> )	γ (kN/m <sup>3</sup> )
Reinforced and retained fill	0	34	18
Foundation soil	10	34	18
Blocks	2.5	34	18

#### **Table 1 Material Properties**



**Figure 1 - Geometry** 

Method	Factor of Safety
SSR	0.92
Bishop	0.87
Spencer	0.91
GLE	0.91

Note: Referee Factor of Safety = 1.02 [Leshchinsky and Han]



Critical SRF: 0.92

Figure 2 – Maximum Shear Strain Plot



Figure 3 – SSR Convergence Graph

This problem is taken from the Number of Tiers case studied in the "Geosynthetic Reinforced Multitiered Walls", a paper by Leshchinsky, D. and Han, J. (2004).

#### Description

Verification problem #94 for Slide2 – A three-tiered wall – is shown in Figure 1. The material properties are presented in Table 1 and the support properties are shown in Table 2. The shear strength of the support is assumed to equal to 80% of the fill strength. The purpose of this verification model is to quantify the effect of number of tiers on the stability characteristic of a multi-tiered wall.

# **Geometry and Properties**

Zone	c (kPa)	$\phi$ ( <sup>0</sup> )	$\gamma$ (kN/m <sup>3</sup> )
Reinforced and retained fill	0	34	18
Foundation soil	10	34	18
Blocks	2.5	34	18

# **Table 1 Material Properties**



**Figure 1 - Geometry** 

Method	Factor of Safety
SSR	1.04
Bishop	0.92
Spencer	0.94
GLE	0.94

Note: Referee Factor of Safety = 1.00 [Leshchinsky and Han]



Figure 2 – Maximum Shear Strain Plot

#### Shear Strength Reduction Critical SRF: 1.04 at Displacement: 0.082 m



Figure 3 – SSR Convergence Graph

This problem is taken from the slope stability problem in the "Comparison of geotechnic softwares", a paper by Pruska, J. (2003).

#### Description

A homogeneous slope with a slope height of 7 m is shown in Figure 1. Five cases with different soil properties were studied. Mohr-Coulomb (M-C) and Drucker-Prager (D-P) failure criteria were used in the analysis. The material properties of all five cases are given in table 1. The results of all cases are compared to those of Z-Soil, Plaxis and Geo FEM.

# **Geometry and Properties**

	Young modulus,	Poisson	Weight,	Cohesion,	Friction	Dilatancy
	E (kPa)	Ratio, v	$\gamma$ (kN/m <sup>3</sup> )	c (kPa)	angle, $\phi$ ( <sup>0</sup> )	angle, $\psi$ ( <sup>0</sup> )
Case 1		0.3	24	20	10	
Case 2		0.35	18	5	10	
Case 3	5,000	0.3	24	20	20	0
Case 4		0.35	18	5	20	
Case 5		0.3	24	20	30	

#### **Table 1 Material Properties**



# **Figure 1 - Geometry**

**Results: Case 1** 

Slide2	RS2		Z-Soil		Plaxis	GEO FEM	
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
1.22	1.22	1.21	1.21	1.19	1.22	1.31	1.2



Figure 2 – Maximum Shear Strain Plot of Case 1



Figure 3 – SSR Convergence Graph of Case 1

**Results: Case 2** 

Slide2	RS2		Z-Soil		Plaxis	GEO FEM	
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
0.66	0.67	0.68	0.71	0.69	0.68	0.73	0.66



Figure 4 – Maximum Shear Strain Plot of Case 2



Figure 5 – SSR Convergence Graph of Case 2

**Results: Case 3** 

Slide2	RS2		Z-Soil		Plaxis	GEO FEM	
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
1.64	1.68	1.62	1.64	1.59	1.65	1.71	1.61



Figure 6 – Maximum Shear Strain Plot of Case 3


Figure 7 – SSR Convergence Graph of Case 3

Slide2	RS2		Z-Soil		Plaxis	GEO	FEM
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
1.02	1.05	1.04	0.95	1.2	0.99	1.17	1.08



Figure 8 – Maximum Shear Strain Plot of Case 4



Figure 9 – SSR Convergence Graph of Case 4

Slide2	RS2		Z-Soil		Plaxis	GEO	FEM
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
2.08	2.14	1.92	1.98	1.8	2.09	2.19	2



Figure 10 – Maximum Shear Strain Plot of Case 5



Figure 11 – SSR Convergence Graph of Case 5

### Introduction

This problem is taken from the slope stability problem in the "Comparison of geotechnic softwares", a paper by Pruska, J. (2003).

### Description

A homogeneous slope with a slope height of 10.5 m is shown in Figure 1. Six cases with different soil properties were studied. Mohr-Coulomb (M-C) and Drucker-Prager (D-P) failure criteria were used in the analysis. The material properties of all six cases are given in table 1. The results of all cases are compared to those of Z-Soil, Plaxis and Geo FEM.

### **Geometry and Properties**

	Young modulus, E (kPa)	Poisson Ratio, v	Weight, $\gamma$ (kN/m <sup>3</sup> )	Cohesion, c (kPa)	Friction angle, $\phi$ ( <sup>0</sup> )	Dilatancy angle, $\psi$ ( <sup>0</sup> )
Case 1		0.35	18	5	10	
Case 2		0.3	24	20	10	
Case 3	5 000	0.35	18	5	20	0
Case 4	3,000	0.3	24	20	20	0
Case 5		0.35	18	5	30	
Case 6		0.3	24	20	30	

### **Table 1 Material Properties**



## **Figure 1 - Geometry**

Slide2	RS2		Z-Soil		Plaxis	GEO	FEM
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
0.44	0.44	0.47	0.46	0.43	0.44	0.48	0.43



Figure 2 – Maximum Shear Strain Plot of Case 1



Figure 3 – SSR Convergence Graph of Case 1

Slide2	RS2		Z-Soil		Plaxis	GEO	FEM
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
0.80	0.79	0.80	0.83	0.81	0.85	0.91	0.82



Figure 4 – Maximum Shear Strain Plot of Case 2



Figure 5 – SSR Convergence Graph of Case 2

Slide2	RS2		Z-Soil		Plaxis	GEO	FEM
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
0.69	0.69	0.74	0.71	0.69	0.71	0.73	0.66



Figure 6 – Maximum Shear Strain Plot of Case 3



Figure 7 – SSR Convergence Graph of Case 3

Slide2	RS2		Z-Soil		Plaxis	GEO	FEM
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
1.10	1.11	1.10	1.14	1.04	1.17	1.18	1.10



Figure 8 – Maximum Shear Strain Plot of Case 4



Figure 9 – SSR Convergence Graph of Case 4.

Slide2	RS2		Z-Soil		Plaxis	GEO	FEM
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
0.95	0.96	0.97	0.98	0.91	0.97	1.03	0.81



Figure 10 – Maximum Shear Strain Plot of Case 5



Figure 11 – SSR Convergence Graph of Case 5

Slide2	RS2		Z-Soil		Plaxis	GEO	FEM
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
1.40	1.42	1.34	1.52	1.44	1.45	1.54	1.46



Figure 12 – Maximum Shear Strain Plot of Case 6



Figure 13 – SSR Convergence Graph of Case 6

### Introduction

This problem is taken from the slope stability problem in the "Comparison of geotechnic softwares", a paper by Pruska, J. (2003).

### Description

A homogeneous slope with a slope height of 14 m is shown in Figure 1. Six cases with different soil properties were studied. Mohr-Coulomb (M-C) and Drucker-Prager (D-P) failure criteria were used in the analysis. The material properties of all six cases are given in table 1. The results of all cases are compared to those of Z-Soil, Plaxis and Geo FEM.

### **Geometry and Properties**

	Young modulus,	Poisson	Weight,	Cohesion,	Friction	Dilatancy
	E (kPa)	Ratio, v	$\gamma$ (kN/m <sup>3</sup> )	c (kPa)	angle, $\phi$ ( <sup>0</sup> )	angle, $\psi$ ( <sup>0</sup> )
Case 1		0.35	18	5	10	
Case 2		0.3	24	20	10	
Case 3	5 000	0.35	18	5	20	0
Case 4	3,000	0.3	24	20	20	0
Case 5		0.35	18	5	30	
Case 6		0.3	24	20	30	

### **Table 1 Material Properties**



## Figure 1 - Geometry

Slide2	RS2		Z-Soil		Plaxis	GEO	FEM
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
0.34	0.33	0.37	0.34	0.32	0.35	0.35	0.31





Figure 2 – Maximum Shear Strain Plot of Case 1

Figure 3 – SSR Convergence Graph of Case 1

Slide2	RS2		Z-Soil		Plaxis	GEO	FEM
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
0.60	0.59	0.60	0.61	0.59	0.59	0.63	0.60





Figure 4 – Maximum Shear Strain Plot of Case 2

Figure 5 – SSR Convergence Graph of Case 2

Slide2	RS2		Z-Soil		Plaxis	GEO FEM	
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
0.53	0.52	0.60	0.54	0.50	0.53	0.59	0.48





Figure 6 – Maximum Shear Strain Plot of Case 3

Figure 7 – SSR Convergence Graph of Case 3

Slide2	RS2		Z-Soil		Plaxis	GEO FEM	
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
0.84	0.83	0.87	0.84	0.81	0.82	0.86	0.82





Figure 8 – Maximum Shear Strain Plot of Case 4

Figure 9 – SSR Convergence Graph of Case 4

Slide2	RS2		Z-Soil		Plaxis	GEO FEM	
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
0.73	0.72	0.80	0.75	0.72	0.74	0.73	0.66





Figure 10 – Maximum Shear Strain Plot of Case 5

Figure 11 – SSR Convergence Graph of Case 5

Slide2	RS2		Z-Soil		Plaxis	GEO FEM	
	M-C	D-P	M-C	D-P	M-C	M-C	D-P
1.08	1.06	1.05	1.07	1.03	1.06	1.10	1.05





Figure 12 – Maximum Shear Strain Plot of Case 6

Figure 13 – SSR Convergence Graph of Case 6

- 1. Duncan, J. M. and Wright, S. G. (2005), "Soil Strength and Slope Stability." John Wiley & Sons, Hoboken, N.J.
- Leshchinsky, D. and Han, J. (2004), "Geosynthetic Reinforced Multitiered Walls." Journal of Geotechnical and Geoenvironmental Engineering. Vol. 130, No. 12, December, pp. 1225-1235.
- 3. Pruska, J. (2003), "Comparison of geotechnic softwares Geo FEM, Plaxis, Z-Soil." Proc. XIII ECSMGE, Vanicek et al. (eds), CGtS, Prague. Vol. 2, August, pp. 819-824.